# Electrical properties of MREGeO<sub>4</sub> (M = Li, Na, K; RE = rare earth) ceramics

YAN LIN AUNG, S. NAKAYAMA Department of Applied Chemistry and Biotechnology, Niihama National College of Technology, Niihama 792-8580, Japan E-mail: nakayama@chem.niihama-nct.ac.jp

M. SAKAMOTO Department of Material & Biological Chemistry, Faculty of Science, Yamagata University, Yamagata 990-8560, Japan

Fourteen kinds of alkali-metal rare earth germanate ceramics, MREGeO<sub>4</sub> (M = Li, Na, K; RE = rare earth), were synthesized and their electrical properties were investigated. The crystal structures of the major phases of MREGeO<sub>4</sub> could be classified into four groups; hexagonal (apatite type), tetragonal, orthorhombic (olivine type) and orthorhombic ( $\beta$ -K<sub>2</sub>SO<sub>4</sub> type). The tetragonal group exhibited higher ionic conductivity than the other groups in the range 300 to 700°C. The highest conductivity was achieved for the LiNdGeO<sub>4</sub> having a tetragonal structure (2.95 × 10<sup>-2</sup> S cm<sup>-1</sup> at 700°C). Analyses on the basis of the Nernst's equation indicated that the two electron reaction associated with carbon dioxide molecule takes place at the detection electrode above 400°C regardless of the kind of electrolyte. The electromotive force, EMF, of the potentiometric CO<sub>2</sub> gas sensors designed using MLaGeO<sub>4</sub> (M = Li, Na, K) increased linearly with an increase in the logarithmic value of CO<sub>2</sub> partial pressure, in accordance with the Nernst equation. © *2005 Springer Science* + *Business Media, Inc.* 

## 1. Introduction

With the development of solid-state batteries and chemical sensors, ionic conductors (solid-state electrolytes) which have higher electrical conductivity and a higher degree of densification are becoming increasingly important because of their suitability for the main components of such batteries and sensors [1, 2]. To develop and improve such ionic conductors, the choice of crystal structures and mobile ions, the addition of modifier ion species and the methods used to increase their density have to be considered [3, 4]. Among the many alkali-metal ionic conductors,  $\beta$ -eucryptite, LiAlSiO<sub>4</sub> is known as a Li ionic conductor possessing a conducting pathway along the minor axis of the hexagonal structure, in which a three-dimensional network is built from interconnected AlO<sub>4</sub> and SiO<sub>4</sub> tetrahedra [5]. Another characteristic of LiAlSiO<sub>4</sub> is a fairly higher resistance to water; when 10 g of a sample sintered at  $1300^{\circ}$ C was immersed in 100 ml of water at room temperature for 24 h, only 22 ppm of Li<sup>+</sup> ion was eluted [6]. In order to develop well compacted alkali-metal ionic conductors with excellent water-resistance and high ionic conductivity, we previously prepared alkali-metal (M) rare-earth (RE) silicates (MRESiO<sub>4</sub>) and investigated their ionic electrical conductivities [7, 8]. These materials can be thought of as a three-dimensional network of interconnected REO<sub>6</sub> octahedra and SiO<sub>4</sub> tetrahedra i.e., using a series of rare earth elements instead of aluminium in LiAlSiO<sub>4</sub>. It was found that the major phase of MRESiO<sub>4</sub> (M = Li, K; RE = La, Nd, Sm, Gd, Dy) ceramics had the hexagonal apatite type structure (space group:P63/m) [9] and these alkali-metal ionic conductors exhibited higher electrical conductivities [10, 11].

In this work, we synthesized alkali based MREGeO<sub>4</sub> (M = Li, Na, K; RE = La, Pr, Nd, Sm, Gd, Dy, Ho, Er, Yb) ceramics in which Ge (ionic radius: 0.040 nm [12]) was substituted for Si (ionic radius: 0.026 nm [12]) in the SiO<sub>4</sub> tetrahedra, in order to gain an information about the size effect of the tetrahedral site. The crystal structures and the electrical properties of these ceramics, compared with MRESiO<sub>4</sub> (M = Li, Na, K) ceramics previously reported [8] were investigated.

### 2. Experimental

Reagent grade  $M_2CO_3$  (M = Li, Na, K), GeO<sub>2</sub> and rareearth oxide RE<sub>2</sub>O<sub>3</sub> (RE = La, Nd, Sm, Gd, Dy, Ho, Er, Yb) or Pr<sub>6</sub>O<sub>11</sub> were ball-milled in a plastic pot with zirconia balls and methanol for 16 h. The mixture was dried in an oven at 80°C and was put into an alumina crucible and calcined in air at 800°C for 2 h. The resultant powder was ball-milled again for 16 h into a fine powder. After being dried, the powder was pressed at 50 MPa into a disc and sintered on a platinum plate at 1050–1150°C (see Table I).

The densities of the sintered products were determined by Archimedes method. The powder X-ray

TABLE I Lattice constants, cell volumes, phases and sintering temperatures

Material	<i>a</i> (nm)	<i>b</i> (nm)	<i>c</i> (nm)	<i>V</i> (nm <sup>3</sup> )	Phase <sup>a</sup>	Sintering temp. (°C)
			MREGeO <sub>4</sub> sy	stem		
LiLaGeO <sub>4</sub>	0.987		0.723	0.609	H(a)	1050
LiPrGeO <sub>4</sub>	0.975		0.709	0.583	H(a)	1050
LiNdGeO <sub>4</sub>	0.742		0.974	0.536	Т	1100
LiSmGeO <sub>4</sub>	0.735		0.965	0.521	Т	1100
LiGdGeO <sub>4</sub>	0.730		0.961	0.512	Т	1100
LiDyGeO <sub>4</sub>	0.507	1.110	0.633	0.354	O(0)	1100
LiHoGeO <sub>4</sub>	0.507	1.110	0.631	0.353	O(0)	1150
LiErGeO <sub>4</sub>	0.504	1.110	0.633	0.352	O(0)	1150
LiYbGeO <sub>4</sub>	0.502	1.094	0.625	0.343	O(0)	1150
NaLaGeO <sub>4</sub>	0.556	1.015	0.711	0.401	O(k)	1100
NaNdGeO <sub>4</sub>	0.550	1.011	0.693	0.385	O(k)	1300
NaSmGeO <sub>4</sub>	0.544	1.036	0.675	0.380	O(k)	1100
KLaGeO <sub>4</sub>	0.989		0.732	0.620	H(a)	1150
KSmGeO <sub>4</sub>	0.581	0.857	0.813	0.405	O(k)	1300
			MRESiO <sub>4</sub> sys	stem		
LiLaSiO <sub>4</sub>	0.969		0.715	0.582	H(a)	1000
LiNdSiO <sub>4</sub>	0.951		0.699	0.552	H(a)	1000
LiSmSiO <sub>4</sub>	0.945		0.691	0.537	H(a)	1000
LiDySiO <sub>4</sub>	0.936		0.676	0.514	H(a)	1000
LiHoSiO <sub>4</sub>	0.499	1.081	0.633	0.336	O(o)	1050
LiErSiO <sub>4</sub>	0.500	1.083	0.630	0.335	O(o)	1200
LiYbSiO <sub>4</sub>	0.493	1.072	0.624	0.327	O(0)	1300
NaLaSiO <sub>4</sub>	0.541	0.948	0.715	0.369	O(k)	1250
NaNdSiO <sub>4</sub>	0.539	0.944	0.699	0.353	O(k)	1250
NaSmSiO <sub>4</sub>	0.535	0.940	0.688	0.346	O(k)	1250
KLaSiO <sub>4</sub>	0.971		0.724	0.591	H(a)	1350
KSmSiO <sub>4</sub>	0.946		0.701	0.543	H(a)	1350

<sup>a</sup>H(a) = hexagonal (apatite type), T = tetragonal, O(o) = orthorhombic (olivine type) and O(k) = orthorhombic ( $\beta$ -K<sub>2</sub>SO<sub>4</sub> type).

diffraction (XRD) measurements were carried out using Cu K<sub> $\alpha$ </sub> radiation in the 2 $\theta$  range of 20 to 60°. After being coated on both sides of the disc with Pt paste, they were baked at 1000°C. The electrical properties were measured in the temperature range of 300 to 700°C, using an impedance-analyzer (HP4194A) in the frequency range of 100 to 10 MHz.

The solid state cell as a  $CO_2$  gas sensor is composed of the following ionic conductor and electrodes:

MLaGeO<sub>4</sub> (M = Li, Na, K) discs were prepared as above then one side was coated with a Pt paste and the other with a Au paste, before the disc was baked at 1000°C. Then, both sides of the disc were connected with Pt wires. An aqueous solution of M<sub>2</sub>CO<sub>3</sub> was applied to the Au detection electrode and the electrode was dried to prepare the solid electrode. The sensor thus designed was fixed on one-end of an alumina pipe with a glass cement so that the Pt counter electrode was on the inside.

The response characteristics were measured using four kinds of standard CO<sub>2</sub> gases with partial pressures of  $1 \times 10^0$ ,  $1 \times 10^1$ ,  $1 \times 10^2$  and  $1 \times 10^3$  Pa, prepared by diluting given amounts of CO<sub>2</sub> with a synthetic air (<2 × 10<sup>-1</sup> Pa CO<sub>2</sub>) purchased from Sumitomo-Seika Inc. Electromotive force, EMF, was measured using an Advantest TR8652 electrometer.

# **3. Results and discussion** 3.1. Crystal structure

Each sample assumed the characteristic color of the component rare earth ion; colorless for the La, Gd, Dy and Yb ceramics, pale yellow for the Sm ceramics, green for the Pr ceramics, greenish yellow for the Ho ceramics and pink for the Er ceramics.

Typical XRD patterns of MREGeO<sub>4</sub> (M = Li, Na, K; RE = La, Pr, Nd, Sm, Gd, Dy, Ho, Er, Yb) are shown in Fig. 1. The crystal structures of the major phase of MREGeO<sub>4</sub> were classified into four



*Figure 1* Typical XRD patterns of: (a) hexagonal apatite-type LiPrGeO<sub>4</sub>, (b) tetragonal LiSmGeO<sub>4</sub>, (c) orthorhombic olivine-type LiDyGeO<sub>4</sub>, and (d) orthorhombic  $\beta$ -K<sub>2</sub>SO<sub>4</sub>-type NaNdGeO<sub>4</sub>.



*Figure 2* (a) Apatite-type crystal structure of MRE<sub>9</sub>(GeO<sub>4</sub>)<sub>6</sub>O<sub>2</sub> proposed for the major phase of LiREGeO<sub>4</sub> (RE = La ~ Pr) and KLaGeO<sub>4</sub>, (b) olivine-type crystal structure of LiREGeO<sub>4</sub> (RE = Dy ~ Yb), and (c)  $\beta$ -K<sub>2</sub>SO<sub>4</sub>-type crystal structure of NaREGeO<sub>4</sub> (RE = La, Nd, Sm) and KSmGeO<sub>4</sub>.

groups: hexagonal (apatite type) for LiREGeO<sub>4</sub> (RE = La-Pr) and KLaGeO<sub>4</sub> [13], tetragonal for LiREGeO<sub>4</sub> (RE = Nd-Gd) [13], orthorhombic (olivine type) for LiREGeO<sub>4</sub> (RE = Dy-Yb) [13], orthorhombic ( $\beta$ -K<sub>2</sub>SO<sub>4</sub> type) for all of NaREGeO<sub>4</sub> (RE = La-Sm), hexagonal (apatite type) for KLaGeO<sub>4</sub> and orthorhombic ( $\beta$ -K<sub>2</sub>SO<sub>4</sub> type) for KSmGeO4 (see Table I). Fig. 2 shows the structural illustrations of hexagonal apatite type, orthorhombic olivine-type and orthorhombic  $\beta$ -K<sub>2</sub>SO<sub>4</sub> type crystals.

The lattice parameters calculated from the XRD patterns of the MREGeO<sub>4</sub> system are also summarized in Table I, together with those of the MRESiO<sub>4</sub> system. The substitution of  $Ge^{4+}$  with an ionic radius of 0.040 nm for Si<sup>4+</sup> with an ionic radius of 0.026 nm is reflected in the increase of cell volume, when MREGeO4 and MRESiO<sub>4</sub> of the same structure are compared. Hexagonal apatite type  $MLaGeO_4(M = Li, K)$  and orthorhombic olivine type LiREGeO<sub>4</sub> (RE = Ho, Er, Yb) have cell volumes of 0.609-0.620 nm<sup>3</sup> and 0.353-0.343 nm<sup>3</sup>, respectively, which are increased by ca. 5% compared with those of the corresponding MLaSiO<sub>4</sub> (M = Li, K) and LiRESiO<sub>4</sub> (RE = Ho, Er, Yb). The cell volumes of orthorhombic  $\beta$ -K<sub>2</sub>SO<sub>4</sub> type NaREGeO<sub>4</sub> (RE = La, Nd, Sm) are in the range of 0.401–0.380 nm<sup>3</sup>, which are 9-10% larger than those of the corresponding NaRESiO<sub>4</sub>.

#### 3.2. Electrical properties

In order to determine the conductivity, complex plane impedance analysis was performed. The typical com-



Figure 3 Relationship between the ionic radii of  $RE^{3+}$  and the electrical conductivities of LiREGeO<sub>4</sub>.

plex impedance plot at the lower temperature gave a semicircle which passes through the *x*-axis near the origin. As the temperature was raised, the semicircle, probably corresponding to the electrolyte itself, diminished and a spike, probably arising from the electrolyte electrode behavior, was observed in the lower frequency region. From these results, the conductivity was determined by the extrapolation to zero reactance of the complex impedance plot. The conductivity data were analysed using the Arrhenius Equation 1.

$$\sigma T = \sigma_0 \exp(-E/kT) \tag{1}$$

where  $\sigma$ ,  $\sigma_0$ , E, k and T are the conductivity, preexponential factor, activation energy, Boltzmann constant and absolute temperature, respectively.

Fig. 3 shows plots of the logarithmic conductivity values of LiREGeO<sub>4</sub> at 300, 500 and 700°C against the ionic radii of the rare earths. The conductivity increased with the rise of temperature, when the same rare earth was used. At a given temperature, the conductivity increased with the increase in ionic radius of  $RE^{3+}$  from Yb to Nd and a steep drop was observed for Pr and La. Conductivities of LiLaGeO<sub>4</sub> and LiPrGeO<sub>4</sub> are lower than LiNdGeO<sub>4</sub> by 1.5 orders of magnitude at 300 and 500°C and one order of magnitude at 700°C. The tetragonal family exhibited higher conductivities than the orthorhombic and hexagonal families in the temperature range of 300 to 700°C. The highest conductivity of  $2.95 \times 10^{-2}$  S cm<sup>-1</sup> was achieved for the tetragonal LiNdGeO<sub>4</sub> at 700°C.

Arrhenius plots of NaREGeO<sub>4</sub> (RE = La, Nd, Sm) and KREGeO<sub>4</sub> (RE = La, Sm) are shown in Fig. 4. The conductivities of orthorhombic  $\beta$ -K<sub>2</sub>SO<sub>4</sub> type NaREGeO<sub>4</sub> (RE = La, Nd, Sm) were higher than those of hexagonal apatite type KLaGeO<sub>4</sub> and orthorhombic  $\beta$ -K<sub>2</sub>SO<sub>4</sub> type KSmGeO<sub>4</sub>.

The effect of alkali metal on the conductivity was examined at 400, 500 and  $600^{\circ}$ C using MLaGeO<sub>4</sub> (M=Li, Na, K). Results are summarized in Fig. 5 which also shows the data of MLaSiO<sub>4</sub> previously



Figure 4 Arrhenius plots for NaREGeO<sub>4</sub> and KREGeO<sub>4</sub>.



*Figure 5* Relationship between the ionic radii of alkali-metal and the conductivities of MLaGeO<sub>4</sub> and MLaSiO<sub>4</sub> (M = Li, Na, K).

reported [8]. The conductivity of MLaGeO<sub>4</sub> increased with the decrease in ionic radius of alkali metal at all temperatures, whereas the previous MLaSiO<sub>4</sub> gave the minimum value for M = Na [8]. Furthermore, the conductivities of NaLaGeO<sub>4</sub> and KLaGeO<sub>4</sub> are lower by 1–2.5 orders of magnitude than those of NaLaSiO<sub>4</sub> and KLaSiO<sub>4</sub> [8]. These lower conductivities cannot be explained by the estimation that the cell volumes of NaLaGeO<sub>4</sub> and KLaGeO<sub>4</sub> are 8.7 and 4.9% larger than those of NaLaSiO<sub>4</sub> and KLaSiO<sub>4</sub>, respectively, since the larger cell volume is generally thought to increase the mobility of the alkali metal ion.

# 3.3. Response characteristics as a $CO_2$ gas sensor

Fig. 6 shows the dependence of EMF on the logarithm of  $CO_2$  partial pressure,  $logP_{CO_2}$ , at 500°C for the  $CO_2$ 



Figure 6 Plots of the sensor EMF as a function of the logarithms of  $CO_2$  partial pressures at 500°C.

gas sensors designed using MLaGeO<sub>4</sub> (M = Li, Na or K). Standard gases were passed through the detection electrode side of the sensors at a flow rate of  $50 \text{ cm}^3$ min<sup>-1</sup>. The EMF of each sensor decreased with increase in  $logP_{CO_2}$  and the dependence of EMF on  $logP_{CO_2}$ obeyed the Nernst equation. In the present apparatus, potentials at a given temperature are almost constant, as the counter electrode is shielded from the detected gas. This indicates that the EMF change is due to the potential change at the detection electrode and hence the electron transfer number at the detection electrode can be estimated from the slope of the straight lines given in Fig. 6. Table II summarizes the estimated slopes and electron transfer numbers, n, which can be approximated as 2 above 400°C, suggesting that the detection above 400°C is accomplished based on the two electron transfer reaction associated with one CO<sub>2</sub> molecule.

The response mechanism of the present  $CO_2$  gas sensor was investigated. The counter electrode is always exposed to a constant atmosphere of  $2.1 \times 10^4$  Pa oxygen partial pressure, and therefore the electrode reaction can be expressed by the following equation.

$$2M^+ + 1/2O_2 + 2e^- = M_2O$$
 (2)

On the other hand, it is assumed that the following reaction occurs at the detection electrode.

$$2M^{+} + CO_{2} + 1/2O_{2} + 2e^{-} = M_{2}CO_{3}$$
 (3)

When the Nernst equation is applied to the above Equations 2 and 3, the potentials of counter electrode,

TABLE II Slopes of sensor EMF vs. log  $P_{CO_2}$  and electron transfer numbers (n)

	slope/mV decade <sup>-1</sup>						
Electrolyte	300°C	400°C	500°C	600°C			
LiLaGeO4 NaLaGeO4 KLaGeO4	45.0 (2.5) 41.5 (2.8) 15.0 (7.6)	57.5 (2.3) 60.0 (2.2) 65.0 (2.1)	70.0 (2.2) 70.0 (2.2) 72.5 (2.1)	90.0 (1.9) 85.4 (2.2) 71.0 (2.4)			

*Ec*, and detection electrode, *Es*, are expressed by the following equations, respectively:

$$Ec = Ec' - (RT/2F) \ln(a_{M_2O}/a_{M^+}^2 \cdot (P_{O_2}^{I})^{1/2})$$
(4)

$$Es = Es' - (RT/2F) \ln(a_{M_2CO_3}/a_{M^+}^2 \cdot (P_{O_2}^{II})^{1/2} \cdot P_{CO_2})$$
(5)

where E', R, T, F,  $a_{M_2CO_3}$ ,  $a_{M_2O}$ ,  $P_{CO_2}$  and  $P_{O_2}$  are standard electrode potential, gas constant, absolute temperature, Faraday constant, activities of  $M_2CO_3$  and  $M_2O$ , and partial pressures of  $CO_2$  and  $O_2$ , respectively. As both Ec' and Es' are constant, the EMF, abbreviated as E, is expressed as follows:

$$E = Es - Ec$$
  
=  $E' - (RT/2F) \ln(a_{M_2CO_3} \cdot (P_{O_2}^{I})^{1/2} / a_{M_2O} \cdot P_{CO_2} \cdot (P_{O_2}^{II})^{1/2})$  (6)

where E' is a constant. When the activities of M<sub>2</sub>CO<sub>3</sub>, M<sub>2</sub>O, P<sup>I</sup><sub>O2</sub> and P<sup>II</sup><sub>O2</sub> are kept constant, the CO<sub>2</sub> concentration can be calculated from *E*. Undoubtedly, the present results can be explained by this Equation 6, as can be seen in Fig. 6.

## 4. Conclusion

A series of MREGeO<sub>4</sub> (M = Li, Na, K; RE = rare earth) ceramics were synthesized, and their crystal structures and electrical properties were investigated. The results are summarized as follows;

(1) The crystal structures of the major phase of LiREGeO<sub>4</sub> ceramics could be classified into three groups: hexagonal (apatite type) for La-Pr, tetragonal for Nd-Gd and orthorhombic (olivine type) for Dy-Yb. The crystal structure of NaREGeO<sub>4</sub> ceramics (RE = La-Sm) was orthorhombic ( $\beta$ -K<sub>2</sub>SO<sub>4</sub>type). The KLaGeO<sub>4</sub> and KSmGeO<sub>4</sub> ceramics have hexagonal (apatite type) and orthorhombic ( $\beta$ -K<sub>2</sub>SO<sub>4</sub> type) structures, respectively.

(2) The substitution of  $Ge^{4+}$  with an ionic radius of 0.040 nm for  $Si^{4+}$  with an ionic radius of 0.026 nm was reflected in the increase in cell volume. The cell volume of the MREGeO<sub>4</sub> was about 5% greater than the MRESiO<sub>4</sub> with the same crystal structure.

(3) In the LiREGeO<sub>4</sub> ceramics, the tetragonal family exhibited higher ionic conductivities than the other families in the temperature range of 300 to 700°C and the LiNdGeO<sub>4</sub> having a tetragonal structure, showed the highest conductivity ( $2.95 \times 10^{-2}$  S cm<sup>-1</sup>) at 700°C. The conductivity of MLaGeO<sub>4</sub> increased with decreasing ionic radius of alkali-metal.

(4) The EMF values of the potentiometric CO<sub>2</sub> gas sensors prepared using MLaGeO<sub>4</sub> (M = Li, Na or K) were correlated with the CO<sub>2</sub> concentrations by the Nernst equation. The number of electrons transferred was estimated to be 2 above 400°C. The response characteristics of the sensor were not influenced by the type of solid electrolyte.

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